# The Open University of Sri Lanka Faculty of Natural Sciences B.Sc/ B. Ed Degree Programme



**Department** 

: Mathematics

Level

: 3

Name of the Examination

: Final Examination

Course Title and - Code

: Basic Statistics - ADU3201/ADU3218

Academic Year

: 2020/21

Date

: 06/12/2021

Time

: 9.30 a.m - 11.30 a.m

Duration

: 2 hours

#### **General Instructions**

- 1. Read all instructions carefully before answering the questions.
- 2. This question paper consists of 6 questions in 5 pages.
- 3. Answer 4 questions only. All questions carry equal marks.
- 4. Answer for each question should commence from a new page.
- 6. Involvement in any activity that is considered as an exam offense will lead to punishment
- 7. Use blue or black ink to answer the questions.
- 8. Clearly state your index number in your answer script

A group of students has carried out a study to identify the factors affecting the unemployment rate in a country. They have collected the information on the following variables.

V<sub>1</sub>: Number of unemployed persons

V<sub>2</sub>:Level of education (1: below G.C.E.(O/L); 2: G.C.E.(O/L); 3: G.C.E.(A/L) or above)

V<sub>3</sub>: Having at least one professional qualification (No; Yes)

V<sub>4</sub>: family monthly income (in rupees)

V<sub>5</sub>: Gender (0 - Male; 1- Female)

- (i) Classify the variables as qualitative or quantitative.
- (ii) Classify the quantitative variables as discrete or continuous.
- (iii) Classify the data as nominal, ordinal, interval or ratio.

A result of the data analysis of the "Labour Force Survey-2010 in Sri Lanka" is given below.

| Level of education   | Unemployment rate |        |  |
|----------------------|-------------------|--------|--|
|                      | Male              | Female |  |
| Below G.C.E.(O/L)    | 2.0               | 4.2    |  |
| G.C.E.(O/L           | 5,6               | 9.6    |  |
| G.C.E.(A/L) or above | 8.0               | 16.7   |  |

(Note: Unemployment rate is the number of unemployed persons as a percentage of the Labour Force)

- (iv) Construct a suitable graph that can be used to examine how the unemployment rate varies with gender and level of qualification.
- (v) Clearly state all the findings from the graphical summary constructed in part (iv).

Vehicles coming to a 4 way junction must go in one of three directions: left, right or straight on. Police officer conducted a survey of vehicles coming from the north. It showed that 40% turn left, 25% turn right and the rest go straight. Assume the drivers of the vehicles choose direction independently of each other.

- (i) Draw a tree diagram to show the possible outcomes for the next two vehicles coming from the north.
- (ii) Using the above diagram, find the probability that
  - a) Both vehicles turn left
  - b) One vehicle turns right and the other goes straight
  - c) Both vehicles go in different directions.
- (iii) One day, 2800 vehicles come to the junction from the north. How many of these would you expect to turn right?

#### **Question 3**

A shop sells three different brands of computers, say A, B and C. Past records indicate that 50% of its computer sales are brand A, 30% are brand B and 20% are brand C. Each manufacturer offers a one-year warranty on parts and labor. It is known that 25% of brand A require warranty repair work, whereas the corresponding percentages for brands B and C are 20% and 10% respectively.

- (i) Find the probability that a randomly selected buyer has bought a brand A computer that will need repair while under warranty?
- (ii) Find the probability that a randomly selected buyer has a computer that will need repair under warranty?
- (iii) If a customer returns to the store with a computer that needs warranty repair, find the probability that it is a brand A computer?
- (iv) If a customer returns to the store with a computer that needs warranty repair, find the probability that it is a brand B or a brand C computer?

- (i) Three coins are tossed and the total number of heads in each toss is observed. Let A be the event that at least one head appears, and B be the event that all coins turn up 'heads' or all turn up 'tails'.
  - a) Write down the sample space S.
  - b) Write down the elements in each of the events A and B.
  - c) Find the P(A), P(B) and  $P(A \cap B)$ .
  - d) Are A and B mutually exclusive? Justify your answer.
- (ii) A manager of a company wishes to issue each employee an identity card with one English letter followed by two digits.
  - a) How many different ID cards could be made?
  - b) What is the probability that a randomly selected identity card will have the same two numbers?
- c) What is the probability that a randomly selected identity card will have first number greater than the second number?

#### **Question 5**

The accompanying table shows the frequencies for the number of hours spent watching TV per day for a sample of children at age 5 years computed from the data collected in a study to investigate the television viewing habits of children in Sri Lanka..

| TV hours per day | Number of children |  |  |
|------------------|--------------------|--|--|
| 0-2              | 34                 |  |  |
| 3-5              | 46                 |  |  |
| 6 - 8            | 62                 |  |  |
| 9 – 11           | 40                 |  |  |
| 12 - 14          | 26                 |  |  |

- (i) Find an estimate for the average number of hours spent to watch TV by a randomly chosen child.
- (ii) Find the median of the data.
- (iii) Based on the two measures computed in parts (i) and (ii), what can you say about the shape of the distribution of the data?
- (iv) Find the relative cumulative frequency corresponding to the third class interval and explain what it measures in relation to this study.
- (v) Estimate the percentage of children who watch TV more than 10 hours per day.

According to the past records, the total number of drivers who are caught with no valid driving license at an inspection point on a given day, X, follows the probability mass function given below.

| x      | 0    | 1    | 2 | 3    | 4    | 5    |
|--------|------|------|---|------|------|------|
| P(X=x) | 0.12 | 0.18 | m | 0.25 | 0.20 | 0.05 |

- (i) Find the value of m.
- (ii) Compute the expected value of X and interpret it in relation to this study.
- (iii) Calculate the standard deviation of X.
- (iv) Find the probability that at least two drivers are caught at the inspection point with no valid driving license on a randomly chosen day.
- (v) Find the probability that X takes a value greater than 2 but less than or equal to 4.