The Open University of Sri Lanka B.Sc./B.Ed. Degree Programme – Level 05 Open Book Test (OBT) – 2023/2024 Applied Mathematics ADU5303- Newtonian Mechanics II Duration: - One Hour

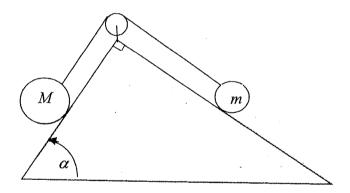


Date: - 29-12-2023

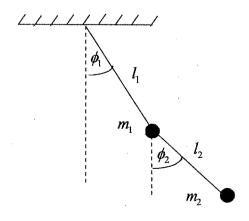
Time :- 4.00 p.m. - 5.00 p.m.

Answer All Questions.

1 Two particles of mass M and m are connected by an inelastic string and placed on two fixed inclined planes as shown in the diagram. The coefficient of friction between the particles and the planes is μ . Using D'Alembert's principle, determine the acceleration of the particles and tension in the string.



2. The double pendulum swinging in a vertical plane consists of two bobs of masses m_1 and m_2 at ends of two weightless rods of lengths l_1 and l_2 and one of them is fixed to a rigid support as shown in figure.



(a) Show that the Lagrangian of the system is given by

$$L = \frac{1}{2} \left(m_1 + m_2 \right) l_1^2 \dot{\phi}_1^2 + \frac{1}{2} m_2 l_2^2 \dot{\phi}_2^2 + m_2 l_1 l_2 \dot{\phi}_1 \dot{\phi}_2 \cos(\phi_1 - \phi_2) + \left(m_1 + m_2 \right) g l_1 \cos \phi_1 + m_2 g l_2 \cos \phi_2$$

(b) Hence, obtain the Lagrange's equations of motion.