

THE OPEN UNIVERSITY OF SRI LANKA  
FACULTY OF MANAGEMENT STUDIES



BACHELOR OF MANAGEMENT STUDIES (HONOURS) DEGREE  
PROGRAMME

OSU 4410 - BUSINESS STATISTICS  
FINAL EXAMINATION – 2024/25  
DURATION – THREE (03) HOURS

DATE: 12<sup>TH</sup> JUNE 2025

TIME: 9.30 AM – 12.30 PM

INSTRUCTIONS:

- Answer FIVE questions ONLY.
- All questions carry equal marks.
- Use of a non-programmable calculator is allowed.
- All workings pertaining to answers should be properly submitted.
- This question paper consists of 6 questions in 10 pages.

**Question 1**

- A. Four percent (4%) of the batteries produced in a factory are defective. If a random sample of 15 batteries is selected from the production line, what is the probability that more than 6 batteries are defective? (4 marks)
- B. A website receives an average of 10 user logins per hour. What is the probability that more than 8 logins occur in a given hour? (4 marks)
- C. Briefly describe the following: (4 marks)
  - i. Normal approximation to Binomial distribution.
  - ii. Normal approximation to Poisson distribution.
- D. In a fishery, the weights of fish caught have a mean of 200 grams and a standard deviation of 30 grams. What is the probability that a randomly selected fish weighs between 150 grams and 180 grams? (4 marks)
- E. According to a Statistics Sourcebook of Criminal Statistics, 7.5% of young adults reported using alcohol daily for the past 30 days. Find the probability that, in a national poll of 1024 young adults, between 40 and 55 inclusive will indicate that they have used alcohol daily for the past 30 days. (4 marks)

**(Total: 20 marks)**

**Question 2**

- A. A random sample of 64 graduate students of a university showed a mean age 27 years and standard deviation of 5 years. Establish a 99% confidence interval of the true mean age of all graduate students at the university. (4 marks)
- B. Briefly describe the following: (10 marks)
- Critical region
  - Null hypothesis
  - Alternative hypothesis
  - Test Statistic
  - Type I error
- C. An inventor has developed a new, energy-efficient machine. He claims that the machine will run continuously for at least 6 hours (360 minutes) on a single gallon of regular gasoline. Suppose a simple random sample of 30 machines is tested. The machines run for an average of 355 minutes, with a standard deviation of 20 minutes. Test the manufacturer's claim at 0.05 level of significance. (6 marks)

**(Total: 20 marks)****Question 3**

Each person in a group of 300 students following a certain study program was identified as male or female and then asked whether he or she preferred taking courses in the areas of Biological Sciences, Physical Sciences, Information Technology, Agriculture, Social Sciences, and Languages. The contingency table below shows the frequencies found for these categories. Does this sample present sufficient evidence to reject the claim that "preference for courses is independent of the gender of a college student"? Consider the .05 level of significance.

| Preferred Course       | Gender |        | Total |
|------------------------|--------|--------|-------|
|                        | Male   | Female |       |
| Biological Sciences    | 17     | 20     | 37    |
| Physical Sciences      | 54     | 14     | 68    |
| Information Technology | 32     | 25     | 57    |
| Agriculture            | 24     | 21     | 45    |
| Social Sciences        | 14     | 23     | 37    |
| Languages              | 21     | 35     | 56    |
| Total                  | 162    | 138    | 300   |

**(Total: 20 marks)**

**Question 4**

A nutritionist wants to study the relationship between weekly vegetable servings and fasting blood glucose levels in women aged 40 years. A sample of 10 women aged 40 was selected. The number of vegetable servings consumed in a typical week and the fasting blood glucose level (in mg/dL) were recorded for each person. The sample data is provided in the table below.

| Number of vegetable servings per week | Fasting blood glucose level (mg/dL) |
|---------------------------------------|-------------------------------------|
| 4                                     | 83                                  |
| 10                                    | 78                                  |
| 2                                     | 100                                 |
| 3                                     | 98                                  |
| 7                                     | 85                                  |
| 5                                     | 86                                  |
| 6                                     | 83                                  |
| 8                                     | 82                                  |
| 2                                     | 102                                 |
| 9                                     | 78                                  |
| Total = 56                            | Total = 875                         |

- Plot the data on a scatter diagram and interpret the relationship you can observe. (5 marks)
- Calculate the correlation between weekly vegetable servings and fasting blood glucose levels in women aged 40 years. Interpret the correlation between the two factors? (5 marks)
- Calculate the regression equation for the scenario. (5 marks)
- If the number of weekly vegetable servings is 5 per week, what amount of fasting blood glucose level would you predict? Compare that result in the table. Why doesn't the regression equation predict the exact value? (5 marks)

**(Total: 20 marks)**

**Question 5**

- A. The marketing manager of a company wants to find whether annual sales made by each sales manager can be predicted based on the years of education and years of experience. The SPSS outputs related to the regression analysis are provided below.

**Coefficients<sup>a</sup>**

| Model               | Unstandardized Coefficients |            | Standardized Coefficients | t       | Sig. |
|---------------------|-----------------------------|------------|---------------------------|---------|------|
|                     | B                           | Std. Error | Beta                      |         |      |
| 1 (Constant)        | -8510.838                   | 586.586    |                           | -14.509 | .000 |
| Years of experience | 1874.500                    | 31.239     | .919                      | 60.005  | .000 |
| Years of education  | 609.391                     | 38.237     | .244                      | 15.937  | .000 |

a. Dependent Variable: Last year sales

- Determine the regression equation based on the output tables given. (3 marks)
- The management of the company claims that the weekly sales increase with the years of experience. Is this statement correct? Justify your answer. (3 marks)
- Interpret the coefficient of the variable of 'years of education'. (Its strength and how it may affect the sales value) (3 marks)

- B. Comment on the correlation coefficient values (i.e. the relationship and its strength) given in the below table at 5% significance level. (8 marks)

| Dimension | Coefficient of correlation with variable E | Sig ( <i>p</i> ) |
|-----------|--------------------------------------------|------------------|
| A         | 0.855                                      | 0.005            |
| B         | -0.362                                     | 0.001            |
| C         | -0.780                                     | 0.078            |
| D         | 0.082                                      | 0.162            |

- C. Briefly discuss the importance of correlation analysis and regression analysis. (3 marks)

**(Total: 20 marks)**

**Question 6**

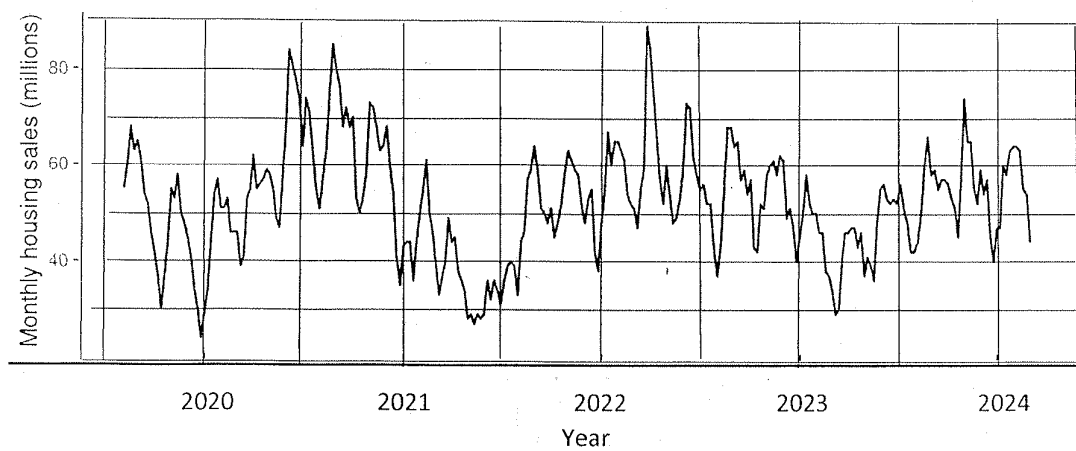
A. The quarterly earnings of a distribution company have been recorded for the period 2021 - 2024. These data (in millions of Rupees) are shown in the accompanying table.

| Period | Year | Quarter | Sales | Quarterly<br>Moving<br>Averages | Centered<br>Moving<br>Averages<br>(CMA) | Sales/<br>CMA |
|--------|------|---------|-------|---------------------------------|-----------------------------------------|---------------|
| 1      | 2021 | 1       | 211   |                                 |                                         |               |
| 2      |      | 2       | 274   |                                 |                                         |               |
| 3      |      | 3       | 235   | 236.75                          | 235.625                                 | 1             |
| 4      |      | 4       | 227   | 234.5                           | 236.375                                 | 0.96          |
| 5      | 2022 | 1       | 202   | (a)                             | 244.75                                  | 0.83          |
| 6      |      | 2       | 289   | (b)                             | 252.375                                 | 1.15          |
| 7      |      | 3       | 287   | (c)                             | (f)                                     | (k)           |
| 8      |      | 4       | 236   | 263.25                          | (g)                                     | (l)           |
| 9      | 2023 | 1       | 241   | 258.75                          | (h)                                     | 0.95          |
| 10     |      | 2       | 271   | 250.75                          | 258.125                                 | 1.05          |
| 11     |      | 3       | 255   | 265.5                           | 265.125                                 | 0.96          |
| 12     |      | 4       | 295   | 264.75                          | 265.875                                 | 1.11          |
| 13     | 2024 | 1       | 238   | 267                             | (i)                                     | (m)           |
| 14     |      | 2       | 280   | (d)                             | (j)                                     | (n)           |
| 15     |      | 3       | 280   | (e)                             |                                         |               |
| 16     |      | 4       | 231   |                                 |                                         |               |

- Calculate the values for (a) – (n). (7 marks)
- Find the adjusted seasonal index values. (5 marks)
- If the trend line equation is,  $\text{Sales} = 237.83 + 1.8 \times \text{Period}$ , find the forecasted sales for the four quarters of year 2025. (4 marks)

B. Interpret the following graph with the knowledge of time series.

(4 marks)



**(Total: 20 marks)**

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Binomial Probability Distribution Table

| n = 15 |          |          |          |          |          |          |          |          |          |
|--------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| x      | p = 0.01 | p = 0.02 | p = 0.03 | p = 0.04 | p = 0.05 | p = 0.06 | p = 0.07 | p = 0.08 | p = 0.09 |
| 0      | 0.8601   | 0.7386   | 0.6333   | 0.5421   | 0.4633   | 0.3953   | 0.3367   | 0.2863   | 0.2430   |
| 1      | 0.1303   | 0.2261   | 0.2938   | 0.3388   | 0.3658   | 0.3785   | 0.3801   | 0.3734   | 0.3605   |
| 2      | 0.0092   | 0.0323   | 0.0636   | 0.0988   | 0.1348   | 0.1691   | 0.2003   | 0.2273   | 0.2496   |
| 3      | 0.0004   | 0.0029   | 0.0085   | 0.0178   | 0.0307   | 0.0468   | 0.0653   | 0.0857   | 0.1070   |
| 4      | 0.0000   | 0.0002   | 0.0008   | 0.0022   | 0.0049   | 0.0090   | 0.0148   | 0.0223   | 0.0317   |
| 5      | 0.0000   | 0.0000   | 0.0001   | 0.0002   | 0.0006   | 0.0013   | 0.0024   | 0.0043   | 0.0069   |
| 6      | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0001   | 0.0003   | 0.0006   | 0.0011   |
| 7      | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0001   | 0.0001   |
| x      | p = 0.99 | p = 0.98 | p = 0.97 | p = 0.96 | p = 0.95 | p = 0.94 | p = 0.93 | p = 0.92 | p = 0.91 |
| 0      | 0.2059   | 0.0874   | 0.0352   | 0.0134   | 0.0047   | 0.0016   | 0.0005   | 0.0001   | 0.0000   |
| 1      | 0.3432   | 0.2312   | 0.1319   | 0.0668   | 0.0305   | 0.0126   | 0.0047   | 0.0016   | 0.0005   |
| 2      | 0.2669   | 0.2856   | 0.2309   | 0.1559   | 0.0916   | 0.0476   | 0.0219   | 0.0090   | 0.0032   |
| 3      | 0.1285   | 0.2184   | 0.2501   | 0.2252   | 0.1700   | 0.1110   | 0.0634   | 0.0318   | 0.0139   |
| 4      | 0.0428   | 0.1156   | 0.1876   | 0.2252   | 0.2186   | 0.1792   | 0.1268   | 0.0780   | 0.0417   |
| 5      | 0.0105   | 0.0449   | 0.1032   | 0.1651   | 0.2061   | 0.2123   | 0.1859   | 0.1404   | 0.0916   |
| 6      | 0.0019   | 0.0132   | 0.0430   | 0.0917   | 0.1472   | 0.1906   | 0.2066   | 0.1914   | 0.1527   |
| 7      | 0.0003   | 0.0030   | 0.0138   | 0.0393   | 0.0811   | 0.1319   | 0.1771   | 0.2013   | 0.1964   |
| 8      | 0.0000   | 0.0005   | 0.0035   | 0.0131   | 0.0348   | 0.0710   | 0.1181   | 0.1647   | 0.1964   |
| 9      | 0.0000   | 0.0001   | 0.0007   | 0.0034   | 0.0116   | 0.0298   | 0.0612   | 0.1048   | 0.1527   |
| 10     | 0.0000   | 0.0000   | 0.0001   | 0.0007   | 0.0030   | 0.0096   | 0.0245   | 0.0515   | 0.0916   |
| 11     | 0.0000   | 0.0000   | 0.0000   | 0.0001   | 0.0006   | 0.0024   | 0.0074   | 0.0191   | 0.0417   |
| 12     | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0001   | 0.0004   | 0.0016   | 0.0052   | 0.0139   |
| 13     | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0001   | 0.0003   | 0.0010   | 0.0032   |
| 14     | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0001   | 0.0005   |
| 15     | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   |
| x      | p = 0.90 | p = 0.85 | p = 0.80 | p = 0.75 | p = 0.70 | p = 0.65 | p = 0.60 | p = 0.55 | p = 0.50 |
| 0      | 0.2059   | 0.0874   | 0.0352   | 0.0134   | 0.0047   | 0.0016   | 0.0005   | 0.0001   | 0.0000   |
| 1      | 0.3432   | 0.2312   | 0.1319   | 0.0668   | 0.0305   | 0.0126   | 0.0047   | 0.0016   | 0.0005   |
| 2      | 0.2669   | 0.2856   | 0.2309   | 0.1559   | 0.0916   | 0.0476   | 0.0219   | 0.0090   | 0.0032   |
| 3      | 0.1285   | 0.2184   | 0.2501   | 0.2252   | 0.1700   | 0.1110   | 0.0634   | 0.0318   | 0.0139   |
| 4      | 0.0428   | 0.1156   | 0.1876   | 0.2252   | 0.2186   | 0.1792   | 0.1268   | 0.0780   | 0.0417   |
| 5      | 0.0105   | 0.0449   | 0.1032   | 0.1651   | 0.2061   | 0.2123   | 0.1859   | 0.1404   | 0.0916   |
| 6      | 0.0019   | 0.0132   | 0.0430   | 0.0917   | 0.1472   | 0.1906   | 0.2066   | 0.1914   | 0.1527   |
| 7      | 0.0003   | 0.0030   | 0.0138   | 0.0393   | 0.0811   | 0.1319   | 0.1771   | 0.2013   | 0.1964   |
| 8      | 0.0000   | 0.0005   | 0.0035   | 0.0131   | 0.0348   | 0.0710   | 0.1181   | 0.1647   | 0.1964   |
| 9      | 0.0000   | 0.0001   | 0.0007   | 0.0034   | 0.0116   | 0.0298   | 0.0612   | 0.1048   | 0.1527   |
| 10     | 0.0000   | 0.0000   | 0.0001   | 0.0007   | 0.0030   | 0.0096   | 0.0245   | 0.0515   | 0.0916   |
| 11     | 0.0000   | 0.0000   | 0.0000   | 0.0001   | 0.0006   | 0.0024   | 0.0074   | 0.0191   | 0.0417   |
| 12     | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0001   | 0.0004   | 0.0016   | 0.0052   | 0.0139   |
| 13     | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0001   | 0.0003   | 0.0010   | 0.0032   |
| 14     | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0001   | 0.0005   |
| 15     | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   | 0.0000   |

$$P(r) = {}^nC_r p^r q^{(n-r)}$$

$$P(x) = \frac{e^{-\lambda} \lambda^x}{x!} \text{ where, } e = 2.718$$

$$\underline{x} \pm z^* \sigma / \sqrt{n}$$

$$\underline{x} \pm t^* s / \sqrt{n}$$

$$P \pm z \sqrt{\frac{p(1-p)}{n}}$$

$$\chi^2 = \sum_{i=1}^k \left[ \frac{(O_i - E_i)^2}{E_i} \right]$$

$$Z = \frac{\underline{x} - \mu}{\frac{\sigma}{\sqrt{n}}}$$

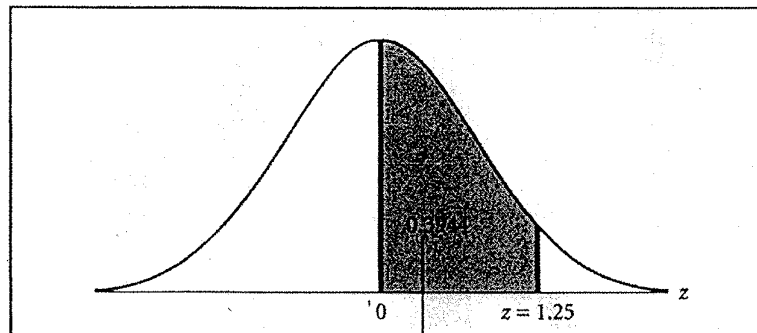
$$Z = \frac{\underline{x}_1 - \underline{x}_2 - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$$

$$r = \frac{\sum xy - \frac{\sum(x) \cdot \sum(y)}{n}}{\sqrt{\left( \sum x^2 - \frac{(\sum x)^2}{n} \right) \left( \sum y^2 - \frac{(\sum y)^2}{n} \right)}}$$

$$b = \frac{n \sum xy - (\sum x)(\sum y)}{n \sum x^2 - (\sum x)^2}$$

$$a = \frac{\sum y}{n} - b \cdot \frac{\sum x}{n}$$

Standard Normal Distribution Table

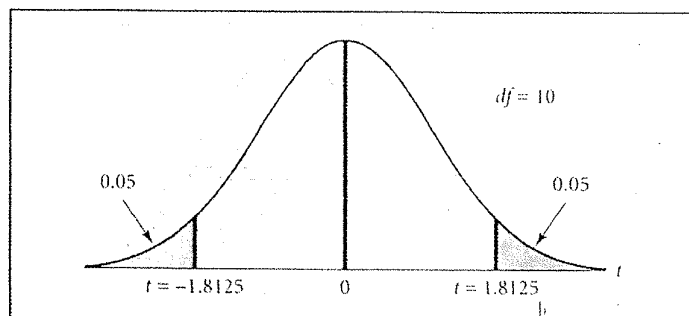


| z   | 0      | 0.01   | 0.02   | 0.03   | 0.04   | 0.05   | 0.06   | 0.07   | 0.08   | 0.09   |
|-----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.0 | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| 0.1 | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| 0.2 | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | 0.1026 | 0.1064 | 0.1103 | 0.1141 |
| 0.3 | 0.1179 | 0.1217 | 0.1255 | 0.1293 | 0.1331 | 0.1368 | 0.1406 | 0.1443 | 0.1480 | 0.1517 |
| 0.4 | 0.1554 | 0.1591 | 0.1628 | 0.1664 | 0.1700 | 0.1736 | 0.1772 | 0.1808 | 0.1844 | 0.1879 |
| 0.5 | 0.1915 | 0.1950 | 0.1985 | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| 0.6 | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | 0.2881 | 0.2910 | 0.2939 | 0.2967 | 0.2995 | 0.3023 | 0.3051 | 0.3078 | 0.3106 | 0.3133 |
| 0.9 | 0.3159 | 0.3186 | 0.3212 | 0.3238 | 0.3264 | 0.3289 | 0.3315 | 0.3340 | 0.3365 | 0.3389 |
| 1.0 | 0.3413 | 0.3438 | 0.3461 | 0.3485 | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| 1.1 | 0.3643 | 0.3665 | 0.3686 | 0.3708 | 0.3729 | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| 1.2 | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | 0.3997 | 0.4015 |
| 1.3 | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | 0.4222 | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| 2.1 | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| 2.2 | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| 2.3 | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| 2.4 | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.5 | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| 2.6 | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| 2.7 | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| 2.9 | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.0 | 0.4987 | 0.4987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.4990 | 0.4990 |

Highlighted value is 0.3944



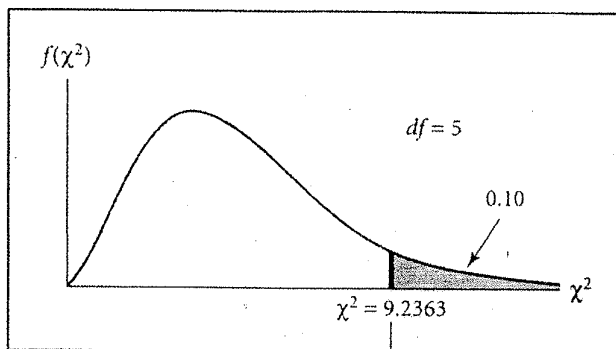
## Critical Values for t- Distribution



| PROBABILITIES (OR AREAS UNDER t-DISTRIBUTION CURVE) |                         |        |        |        |        |        |         |         |         |
|-----------------------------------------------------|-------------------------|--------|--------|--------|--------|--------|---------|---------|---------|
| Conf. Level                                         | 0.1                     | 0.3    | 0.5    | 0.7    | 0.8    | 0.9    | 0.95    | 0.98    | 0.99    |
| One Tail                                            | 0.45                    | 0.35   | 0.25   | 0.15   | 0.1    | 0.05   | 0.025   | 0.01    | 0.005   |
| Two Tails                                           | 0.9                     | 0.7    | 0.5    | 0.3    | 0.2    | 0.1    | 0.05    | 0.02    | 0.01    |
| df                                                  | Values of t             |        |        |        |        |        |         |         |         |
| 1                                                   | 0.1584                  | 0.5095 | 1.0000 | 1.9626 | 3.0777 | 6.3137 | 12.7062 | 31.8210 | 63.6559 |
| 2                                                   | 0.1421                  | 0.4447 | 0.8165 | 1.3862 | 1.8856 | 2.9200 | 4.3027  | 6.9645  | 9.9250  |
| 3                                                   | 0.1366                  | 0.4242 | 0.7649 | 1.2498 | 1.6377 | 2.3534 | 3.1824  | 4.5407  | 5.8408  |
| 4                                                   | 0.1338                  | 0.4142 | 0.7407 | 1.1896 | 1.5332 | 2.1318 | 2.7765  | 3.7469  | 4.6041  |
| 5                                                   | 0.1322                  | 0.4082 | 0.7267 | 1.1558 | 1.4759 | 2.0150 | 2.5706  | 3.3649  | 4.0321  |
| 6                                                   | 0.1311                  | 0.4043 | 0.7176 | 1.1342 | 1.4398 | 1.9432 | 2.4469  | 3.1427  | 3.7074  |
| 7                                                   | 0.1303                  | 0.4015 | 0.7111 | 1.1192 | 1.4149 | 1.8946 | 2.3646  | 2.9979  | 3.4995  |
| 8                                                   | 0.1297                  | 0.3995 | 0.7064 | 1.1081 | 1.3968 | 1.8595 | 2.3060  | 2.8965  | 3.3554  |
| 9                                                   | 0.1293                  | 0.3979 | 0.7027 | 1.0997 | 1.3830 | 1.8331 | 2.2622  | 2.8214  | 3.2498  |
| 10                                                  | 0.1289                  | 0.3966 | 0.6998 | 1.0931 | 1.3722 | 1.8125 | 2.2281  | 2.7638  | 3.1693  |
| 11                                                  | 0.1286                  | 0.3956 | 0.6974 | 1.0877 | 1.3634 | 1.7959 | 2.2010  | 2.7181  | 3.1058  |
| 12                                                  | 0.1283                  | 0.3947 | 0.6955 | 1.0832 | 1.3562 | 1.7823 | 2.1788  | 2.6810  | 3.0545  |
| 13                                                  | 0.1281                  | 0.3940 | 0.6938 | 1.0795 | 1.3502 | 1.7709 | 2.1604  | 2.6503  | 3.0123  |
| 14                                                  | 0.1280                  | 0.3933 | 0.6924 | 1.0763 | 1.3450 | 1.7613 | 2.1448  | 2.6245  | 2.9768  |
| 15                                                  | 0.1278                  | 0.3928 | 0.6912 | 1.0735 | 1.3406 | 1.7531 | 2.1315  | 2.6025  | 2.9467  |
| 16                                                  | 0.1277                  | 0.3923 | 0.6901 | 1.0711 | 1.3368 | 1.7459 | 2.1199  | 2.5835  | 2.9208  |
| 17                                                  | 0.1276                  | 0.3919 | 0.6892 | 1.0690 | 1.3334 | 1.7396 | 2.1098  | 2.5669  | 2.8982  |
| 18                                                  | 0.1274                  | 0.3915 | 0.6884 | 1.0672 | 1.3304 | 1.7341 | 2.1009  | 2.5524  | 2.8784  |
| 19                                                  | 0.1274                  | 0.3912 | 0.6876 | 1.0655 | 1.3277 | 1.7291 | 2.0930  | 2.5395  | 2.8609  |
| 20                                                  | 0.1273                  | 0.3909 | 0.6870 | 1.0640 | 1.3253 | 1.7247 | 2.0860  | 2.5280  | 2.8453  |
| 21                                                  | 0.1272                  | 0.3906 | 0.6864 | 1.0627 | 1.3232 | 1.7207 | 2.0796  | 2.5176  | 2.8314  |
| 22                                                  | 0.1271                  | 0.3904 | 0.6858 | 1.0614 | 1.3212 | 1.7171 | 2.0739  | 2.5083  | 2.8188  |
| 23                                                  | 0.1271                  | 0.3902 | 0.6853 | 1.0603 | 1.3195 | 1.7139 | 2.0687  | 2.4999  | 2.8073  |
| 24                                                  | 0.1270                  | 0.3900 | 0.6848 | 1.0593 | 1.3178 | 1.7109 | 2.0639  | 2.4922  | 2.7970  |
| 25                                                  | 0.1269                  | 0.3898 | 0.6844 | 1.0584 | 1.3163 | 1.7081 | 2.0595  | 2.4851  | 2.7874  |
| 26                                                  | 0.1269                  | 0.3896 | 0.6840 | 1.0575 | 1.3150 | 1.7056 | 2.0555  | 2.4786  | 2.7787  |
| 27                                                  | 0.1268                  | 0.3894 | 0.6837 | 1.0567 | 1.3137 | 1.7033 | 2.0518  | 2.4727  | 2.7707  |
| 28                                                  | 0.1268                  | 0.3893 | 0.6834 | 1.0560 | 1.3125 | 1.7011 | 2.0484  | 2.4671  | 2.7633  |
| 29                                                  | 0.1268                  | 0.3892 | 0.6830 | 1.0553 | 1.3114 | 1.6991 | 2.0452  | 2.4620  | 2.7564  |
| 30                                                  | 0.1267                  | 0.3890 | 0.6828 | 1.0547 | 1.3104 | 1.6973 | 2.0423  | 2.4573  | 2.7500  |
| 40                                                  | 0.1265                  | 0.3881 | 0.6807 | 1.0500 | 1.3031 | 1.6839 | 2.0211  | 2.4233  | 2.7045  |
| 50                                                  | 0.1263                  | 0.3875 | 0.6794 | 1.0473 | 1.2987 | 1.6759 | 2.0086  | 2.4033  | 2.6778  |
| 60                                                  | 0.1262                  | 0.3872 | 0.6786 | 1.0455 | 1.2958 | 1.6706 | 2.0003  | 2.3901  | 2.6603  |
| 70                                                  | 0.1261                  | 0.3869 | 0.6780 | 1.0442 | 1.2938 | 1.6669 | 1.9944  | 2.3808  | 2.6479  |
| 80                                                  | 0.1261                  | 0.3867 | 0.6776 | 1.0432 | 1.2922 | 1.6641 | 1.9901  | 2.3739  | 2.6387  |
| 90                                                  | 0.1260                  | 0.3866 | 0.6772 | 1.0424 | 1.2910 | 1.6620 | 1.9867  | 2.3685  | 2.6316  |
| 100                                                 | 0.1260                  | 0.3864 | 0.6770 | 1.0418 | 1.2901 | 1.6602 | 1.9840  | 2.3642  | 2.6259  |
| 250                                                 | 0.1258                  | 0.3858 | 0.6755 | 1.0386 | 1.2849 | 1.6510 | 1.9695  | 2.3414  | 2.5956  |
| 500                                                 | 0.1257                  | 0.3855 | 0.6750 | 1.0375 | 1.2832 | 1.6479 | 1.9647  | 2.3338  | 2.5857  |
| ∞                                                   | See Normal Distribution |        |        |        |        |        |         |         |         |

Highlighted value is 1.8125

## Critical Values for Chi-Squared Distribution



PROBABILITIES (OR AREAS UNDER CHI-SQUARE DISTRIBUTION CURVE  
ABOVE GIVEN CHI-SQUARE VALUES)

|           | 0.995                        | 0.99    | 0.975   | 0.95    | 0.90    | 0.10    | 0.05    | 0.025   | 0.01    | 0.005   |
|-----------|------------------------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| <i>df</i> | <i>Values of Chi-Squared</i> |         |         |         |         |         |         |         |         |         |
| 1         | 0.0000                       | 0.0002  | 0.0010  | 0.0039  | 0.0158  | 2.7055  | 3.8415  | 5.0239  | 6.6349  | 7.8794  |
| 2         | 0.0100                       | 0.0201  | 0.0506  | 0.1026  | 0.2107  | 4.6052  | 5.9915  | 7.3778  | 9.2104  | 10.5965 |
| 3         | 0.0717                       | 0.1148  | 0.2158  | 0.3518  | 0.5844  | 6.2514  | 7.8147  | 9.3484  | 11.3449 | 12.8381 |
| 4         | 0.2070                       | 0.2971  | 0.4844  | 0.7107  | 1.0636  | 7.7794  | 9.4877  | 11.1433 | 13.2767 | 14.8602 |
| 5         | 0.4118                       | 0.5543  | 0.8312  | 1.1455  | 1.6103  | 9.2363  | 11.0705 | 12.8325 | 15.0863 | 16.7496 |
| 6         | 0.6757                       | 0.8721  | 1.2373  | 1.6354  | 2.2041  | 10.6446 | 12.5916 | 14.4494 | 16.8119 | 18.5475 |
| 7         | 0.9893                       | 1.2390  | 1.6899  | 2.1673  | 2.8331  | 12.0170 | 14.0671 | 16.0128 | 18.4753 | 20.2777 |
| 8         | 1.3444                       | 1.6465  | 2.1797  | 2.7326  | 3.4895  | 13.3616 | 15.5073 | 17.5345 | 20.0902 | 21.9549 |
| 9         | 1.7349                       | 2.0879  | 2.7004  | 3.3251  | 4.1682  | 14.6837 | 16.9190 | 19.0228 | 21.6660 | 23.5893 |
| 10        | 2.1558                       | 2.5582  | 3.2470  | 3.9403  | 4.8652  | 15.9872 | 18.3070 | 20.4832 | 23.2093 | 25.1881 |
| 11        | 2.6032                       | 3.0535  | 3.8157  | 4.5748  | 5.5778  | 17.2750 | 19.6752 | 21.9200 | 24.7250 | 26.7569 |
| 12        | 3.0738                       | 3.5706  | 4.4038  | 5.2260  | 6.3038  | 18.5493 | 21.0261 | 23.3367 | 26.2170 | 28.2997 |
| 13        | 3.5650                       | 4.1069  | 5.0087  | 5.8919  | 7.0415  | 19.8119 | 22.3620 | 24.7356 | 27.6882 | 29.8193 |
| 14        | 4.0747                       | 4.6604  | 5.6287  | 6.5706  | 7.7895  | 21.0641 | 23.6848 | 26.1189 | 29.1412 | 31.3194 |
| 15        | 4.6009                       | 5.2294  | 6.2621  | 7.2609  | 8.5468  | 22.3071 | 24.9958 | 27.4884 | 30.5780 | 32.8015 |
| 16        | 5.1422                       | 5.8122  | 6.9077  | 7.9616  | 9.3122  | 23.5418 | 26.2962 | 28.8453 | 31.9999 | 34.2671 |
| 17        | 5.6973                       | 6.4077  | 7.5642  | 8.6718  | 10.0852 | 24.7690 | 27.5871 | 30.1910 | 33.4087 | 35.7184 |
| 18        | 6.2648                       | 7.0149  | 8.2307  | 9.3904  | 10.8649 | 25.9894 | 28.8693 | 31.5264 | 34.8052 | 37.1564 |
| 19        | 6.8439                       | 7.6327  | 8.9065  | 10.1170 | 11.6509 | 27.2036 | 30.1435 | 32.8523 | 36.1908 | 38.5821 |
| 20        | 7.4338                       | 8.2604  | 9.5908  | 10.8508 | 12.4426 | 28.4120 | 31.4104 | 34.1696 | 37.5663 | 39.9969 |
| 21        | 8.0336                       | 8.8972  | 10.2829 | 11.5913 | 13.2396 | 29.6151 | 32.6706 | 35.4789 | 38.9322 | 41.4009 |
| 22        | 8.6427                       | 9.5425  | 10.9823 | 12.3380 | 14.0415 | 30.8133 | 33.9245 | 36.7807 | 40.2894 | 42.7957 |
| 23        | 9.2604                       | 10.1957 | 11.6885 | 13.0905 | 14.8480 | 32.0069 | 35.1725 | 38.0756 | 41.6383 | 44.1814 |
| 24        | 9.8862                       | 10.8563 | 12.4011 | 13.8484 | 15.6587 | 33.1962 | 36.4150 | 39.3641 | 42.9798 | 45.5584 |
| 25        | 10.5196                      | 11.5240 | 13.1197 | 14.6114 | 16.4734 | 34.3816 | 37.6525 | 40.6465 | 44.3140 | 46.9280 |
| 26        | 11.1602                      | 12.1982 | 13.8439 | 15.3792 | 17.2919 | 35.5632 | 38.8851 | 41.9231 | 45.6416 | 48.2898 |
| 27        | 11.8077                      | 12.8785 | 14.5734 | 16.1514 | 18.1139 | 36.7412 | 40.1133 | 43.1945 | 46.9628 | 49.6450 |
| 28        | 12.4613                      | 13.5647 | 15.3079 | 16.9279 | 18.9392 | 37.9159 | 41.3372 | 44.4608 | 48.2782 | 50.9936 |
| 29        | 13.1211                      | 14.2564 | 16.0471 | 17.7084 | 19.7677 | 39.0875 | 42.5569 | 45.7223 | 49.5878 | 52.3355 |
| 30        | 13.7867                      | 14.9535 | 16.7908 | 18.4927 | 20.5992 | 40.2560 | 43.7730 | 46.9792 | 50.8922 | 53.6719 |

Highlighted value is 9.2363