

(2) A self-service store employs one cashier at its counter. Nine customers arrive, on an average, every 5 minutes while the cashier can serve 10 customers in 5 minutes. By assuming Poisson distribution for arrival rate and exponential distribution for service rate, find

- (i) the probability that a customer arriving at the store will have to wait.
- (ii) the average length of the queue that forms.
- (iii) the average time a customer spends in the system.
- (iv) the probability that there will be three or more customers waiting for the service.
- (v) the fraction of the time that there are no customers.

**Formulas (in the usual notation)**

**(M/M/1):(∞/FIFO) & (M/M/1):(∞/SIRO) Queuing Systems**

$$P_n = \left(\frac{\lambda}{\mu}\right)^n \left(1 - \frac{\lambda}{\mu}\right)$$

$$P(\text{queue size} \geq n) = \rho^n$$

$$E(n) = \frac{\lambda}{\mu - \lambda}$$

$$E(m) = \frac{\lambda^2}{\mu(\mu - \lambda)}$$

$$V(n) = \frac{\lambda\mu}{(\mu - \lambda)^2}$$

$$E(w) = \frac{\lambda}{\mu(\mu - \lambda)}$$

$$E(v) = \frac{1}{\mu - \lambda}$$

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THE OPEN UNIVERSITY OF SRI LANKA  
 B.Sc. /B.Ed. DEGREE PROGRAMME  
 APPLIED MATHEMATICS-LEVEL 05  
 ADU5304 – OPERATIONAL RESEARCH  
 OPEN BOOK TEST 2017/2018  
**Duration: One Hour**



**Date: 12.01.2019**

**Time: 04.00 p.m- 05.00 p.m**

**Answer all questions**

**(1) Part A**

There are two players in a game, say player  $A$  and player  $B$ . Player  $A$  has Rs.2 coin and Rs.5 coin, and player  $B$  has Rs.1 coin and Rs.10 coin. Each player selects a coin from the other player without knowing what coin the other player has selected. If the total rupees of the coins selected is odd, player  $A$  gets a payoff worth of two coins that were selected, but if the total is even, player  $B$  gets a payoff worth of the two coins.

- (i) Construct the payoff matrix with respect to the player  $A$ .
- (ii) Is there a saddle point? Justify your answer.
- (iii) Determine the optimal strategies for player  $A$  and player  $B$ .
- (iv) Find the value of the game.

**Part B**

Determine the ranges of values of  $\lambda$  and  $\mu$  that will make the position  $(2, 2)$  a saddle point for the game having the payoff matrix given below:

		Player $B$		
		$B_1$	$B_2$	$B_3$
Player $A$	$A_1$	1	3	5
	$A_2$	8	4	$\lambda$
	$A_3$	2	$\mu$	9