

**THE OPEN UNIVERSITY OF SRI LANKA**  
**BACHELOR OF MANAGEMENT STUDIES DEGREE PROGRAMME**  
**LEVEL 06 - ASSIGNMENT TEST 2015/16**  
**OPERATION RESEARCH - MCU 4202**  
**DURATION: TWO (02) HOURS**



**DATE: 27.09.2015**

**TIME: 10.00 am – 12.00 noon**

**ANSWER THREE QUESTIONS ONLY.**  
**ALL QUESTIONS CARRY EQUAL MARKS.**

(01) Four projects  $P_1, P_2, P_3$  and  $P_4$  are to be implemented. These projects could be implemented in any of the four locations  $L_1, L_2, L_3$  or  $L_4$ . But the labor requirement would depend on the particular project and the location it is assigned, as shown in the table below.

**Labor Requirement**

	$L_1$	$L_2$	$L_3$	$L_4$
$P_1$	12	17	14	15
$P_2$	7	6	8	9
$P_3$	21	15	27	20
$P_4$	15	11	17	18

- Find the optimal plan of assignment projects to location that would minimize the total labor requirement.
- Find the optimal plan of assigning project to locations given that project  $P_2$  should not be assigned to location  $L_3$ .

(02) A project consists of six activities, A, B, C, .... F whose precedence and durations are explained in the table below.

ACTIVITY	PRECEDENCE	DURATION (DAYS)
A	Project Start	5
B	Project Start	6
C	After "A"	6
D	After "A"	8
E	After "B" and "D"	7
F	After "C" and "E"	5

- (i) Construct the network.
  - (ii) Time analyze and find the float of each activity.
  - (iii) Name the critical path.
  - (iv) Calculate EST, EFT, LFT and LST of each activity.
  - (v) What is the earliest project completion time?
- (03) At a laboratory blood samples are received in a poisson fashion at the rate of 8 per hour. There is only one technologist who on the average takes 6 minutes to test one blood sample. The laboratory works 10 hours a day.
- (i) How many hours does the technologist idle per day?
  - (ii) What is the probability that there are three blood samples at the laboratory?
  - (iii) On the average how many blood samples are there in the laboratory?
  - (iv) How long will a blood sample have to be kept at the laboratory?
  - (v) On the average how many blood samples are there waiting to be tested in the laboratory?
  - (vi) How long must a blood sample be kept until it is taken for testing?
  - (vii) Blood samples, as they are received are put in a freezer that has a capacity to hold 8 blood samples. If the freezer is full the sample is kept out side. What is a probability that a blood sample just received is kept outside the freezer?
- (04) Sanjeeva company has three factories A, B and C that turns out gas cookers. The weekly capacities of the factories A, B and C are 5000, 6000 and 2500 respectively. These cookers are transported to four distribution centers P, Q, R and S whose weekly demands are 6000, 4000, 2000 and 1500. The cost of transporting one unit from a given factory to a given distribution center is explained in the table below.

**Cost of Installation (Rs. 000)**

FACTORY	DISTRIBUTION CENTRE			
	P	Q	R	S
A	3	2	7	6
B	7	5	2	3
C	2	5	4	5

Sanjeeva company wishes to develop the transportation plan that would minimize total cost of transport.

- (i) Find an initial feasible solution using north-west or least cost method.
- (ii) Solve the transportation problem using either MODI method or stepping stone method.

(05) Write short notes on the following with suitable illustrations.

- a) Critical Path
- b) Balanced Transportation Problem
- c) Limitations of Assignment Theory
- d) North West Corner Rule Method
- e) Advantages of graphical method and simplex method in solving Linear Programming problems

**Formulae**

$\lambda$  = Rate of arrival of units

$\mu$  = Rate of service completion

$\theta$  =  $\lambda/\mu$

H = Number of working hours per day

$P_{(n)}$  = Probability of "n" units in the queuing system

$L_s$  = Average number of units in queuing system

$L_q$  = Average number of units in queue

$W_s$  = Average time spent by units in queuing system

$W_q$  = Average time spent by units in queue

$P(n) = \theta P(n-1)$  ————— (1)

$P(n) = \theta^n P(0)$  ————— (2)

$P(n) = \theta^n (1-\theta)$  ————— (3)

(Probability that queuing system empty) =  $(1 - \theta)$  ————— (4)

(Probability that the server is idle) =  $(1 - \theta)$  ————— (5)

(Number of hours server idle per day) =  $H(1 - \theta)$  ————— (5)

$L_s = \theta/(1 - \theta)$  ————— (7)

$L_q = \theta^2/(1 - \theta)$  ————— (8)

$L_s = \lambda W_s$  ————— (9)

$L_q = \lambda W_q$  ————— (10)