The Open University of Sri Lanka Department of Mathematics B.Sc/ B.Ed Degree Programme No Book Test (NBT) - 2016/2017 Applied Mathematics—Level 05 APU3244 – Graph Theory



## **DURATION: - ONE AND HALF HOURS**

Date: - 05 - 11 - 2017

Time: -04.00 p.m. - 05.30 p.m.

## ANSWER ALL QUESTIONS. THE TOTAL MAXIMUM MARK ATTAINABLE IS 200 AND THE FINAL MARK WILL BE CONVERTED TO 100%.

- 01. In each of the following cases, draw a graph which satisfies those conditions:
  - (a) A non-Eulerian graph that is orientable,

[10 Marks]

(b) A non-Hamiltonian tournament that is semi-Hamiltonian,

[15 Marks]

(c) A strongly connected tournament that is Hamiltonian,

[15 Marks]

(d) A connected graph that is isomorphic to its line graph,

[10 Marks]

(e) A graph which is both *Eulerian* and *Hamiltonian* so that its *line graph* is also both *Eulerian* and *Hamiltonian*.

[10 Marks]

- 02. Let  $E = \{1, 2, 3, 4, 5, 6\}$  and let  $S_1 = \{2, 3\}$ ,  $S_2 = \{2, 3\}$ ,  $S_3 = \{1, 2\}$ ,  $S_4 = \{1, 2\}$  and  $S_5 = \{1, 4, 5, 6\}$ .
  - (a) Determine whether  $\mathfrak{I} = (S_1, \ldots, S_5)$  has transversal or not. Justify your answer,
  - (b) List three partial transversals of  $\mathfrak{I}' = (S_1, S_2, S_3, S_5)$ ,

[15 Marks]

[15 Marks]

(c) Write down the incidence matrix A of the family  $\Im$ .

[10 Marks]

Hence, find the term rank,

[05 Marks]

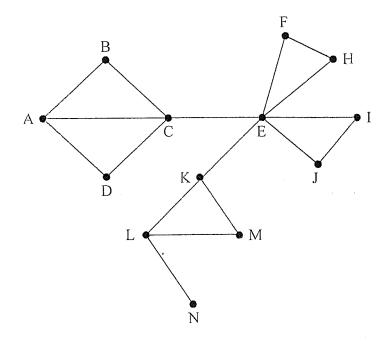
(d) Verify the Kong-Egervacy theorem for the incidence matrix A.

[15 Marks]

Hence, verify your result obtained in part (a).

[15 Marks]

## 03. Let G be the following graph.



Find all the cut points in G and draw the cut point graph, (a)

How many bridges are in G? Justify your answer, (b)

[20 Marks]

[20 Marks]

Find all blocks of G and draw the block graph. (c)