

The Open University of Sri Lanka  
 B.Sc/B.Ed. DEGREE, CONTINUING EDUCATION PROGRAMME  
 OPEN BOOK TEST (OBT) 2010/2011  
 Level 04 Applied mathematics  
 APU 2140- Statistical Distribution Theory



Duration: - One and Half Hours.

DATE: - 09-09-2010.

Time: - 4.00 p.m. – 5.30 p.m.

Non programmable calculators are permitted. Statistical tables are provided.

Answer All Questions.

(1)

A company that produces a certain electrical product claims that the life time of the product  $X$  (in years ) has the density function.

$$f_X(x) = ke^{-kx}; x > 0, k > 0$$

The past data indicate that it is reasonable to take that the median of the lifetime to be five years.

- (a) Calculate the value  $k$ .
- (b) Find the mean lifetime of the product.
- (c) What is the probability that a randomly selected product will fail within 7 years?
- (d) Find the variance of the lifetime of the product.

(2)

A newly married couple decides to have children until they have three children of the same sex. Assume that  $\Pr(\text{Male birth}) = \Pr(\text{Female birth}) = 0.5$ . Let  $X$  be the number of children in the family at the end.

- (a) Write down the possible values for  $X$
- (b) Find the probability mass function of  $X$ .
- (c) Find the probability that there will be less than four children in the family.
- (d) What is the expected number of children in the family?

- (e) Suppose another married couple decides the same rule given above regarding the number of children they wish. What is the expected number of total children in the two families?

(3)

- (a) Explain the distinctive features of Binomial and Poisson distributions.
- (b) Some traffic lights have three phases: *stop* 45% of the time, *wait or get ready* 10% of the time and *go* 45% of the time. Assuming that you only cross a traffic light when it is in the *go* position and that you have to pass 8 such traffic lights on your way to school, model the number of times that you have to *wait or stop* on your way to school.  
State any assumptions that must be made and give possible values for the parameters  $n$  and  $p$ .

Hence find the mean number of times that you have to *wait or stop* on your way to school.

- (c) The number of admissions to an emergency ward of a hospital on a Saturday morning during the period beginning at 12.00 midnight and ending at 2.00 a.m. is found to have a Poisson distribution with an average of 3.5 admissions. During this period of a particular Saturday morning.
- (i) What is the probability that none will be admitted?
  - (ii) What is the probability that two to six persons (inclusive) will be admitted?