

he Open University of Sri Lanka

Sc. Degree Programme: Level - 05

nal Examination - 2007

SU 3275/PMU3293/PME5293 - Automata Theory -Paper II

uration: Two and Half Hours.

ate: 18.06.2007

1.30 pm - 4.00 pm

nswer Four Questions Only.

- a) State the necessary condition for the non-trivial parallel decomposition.
 - b) What do you mean by the term 'non trivial' in the above part a)?
 - c) "Trivial partitions cannot be used for decomposition". Is this statement correct? Justify your answer.
- ii) Draw a DFA that acts as a parity checker. [Hint: parity checker's role is to add one (1) to the odd stream to make it even.]
- i) Define the SP property of a partition.
- ii) Given below is a transition table of a Mealy machine M.

| | | State Transition | | | | Output Transition | | | | |
|---|---|------------------|---|---|---|-------------------|---|---|----|---|
| | 1 | 2 | 3 | 4 | 5 | 1 | 2 | 3 | 4 | 5 |
| a | a | c | a | e | b | 1 | 0 | 1 | 0 | 0 |
| b | C | С | a | е | d | 1 | 0 | 1 | 0_ | 0 |
| c | b | С | a | е | b | 1 | 0 | 0 | 1 | 0 |
| d | b | a | c | a | b | 1 | 0 | 0 | 1_ | 1 |
| e | c | е | a | е | b | 0 | 1 | 1 | 0 | 1 |

- a) Find the SP Partitions of M.
- b) Hence, decompose M parallely.
- c) If you are to decompose M serially what are the additional features you need to know?
- 3. i) Prove for any three Mealy machines M1, M2 and M3 where $k1: O_1 \rightarrow I_2$ $k2: O_2 \rightarrow I_3$ are defined. Show that the following are true.
 - a) $M1 \oplus_{k1} (M2 \oplus_{k2} M3) \leq (M1 \oplus_{k1} M2) \oplus_{k2} M3$
 - b) $M1 \parallel (M2 \parallel M3) \le (M1 \parallel M2) \parallel M3$
 - ii) Suppose M1 and M2 are two Mealy machines.
 - a) Show that $(M1 || M2) \approx (M2 || M1)$.
 - b) Is $(M1 \oplus_{k_1}M2) \approx (M2 \oplus_{k_2}M1)$, where k1: $O_1 \rightarrow I_2$ and k2: $O_2 \rightarrow I_1$? Justify your answer.
- 4. i) Consider the recursive definition of the language L given below.

 L consists of all stings over {0,1} obtained from the basis step by a finite number of applications of the recursive step.

Basis: The empty string ε in L. Recursive: If $x \in L$ then 1x0 is in L.

Prove, by induction, that $L = \{1^i \ 0^j | i \ge j \ge 0\}$.

- ii) a) Construct a DFA that accepts strings over the alphabet {0,1} that have at least one 1 and an even number of 0s after the last 1.
 - b) A DFA has to be constructed for accepting all the words that have $(10101)^n$ 01 as a string, where n is a positive integer. How would you do this construction if the input alphabet is $\{0,1\}$?

- i) Compare the differences of states, inputs, outputs and state/output transition of two mealy machines in parallel and serial composition.
- ii) The following is a transition table of the Mealy machines M1 and M2.

M1

| | 1 | 2 | 1 | 2 |
|----|----|----|---|---|
| S1 | S2 | S3 | Ъ | a |
| S2 | S1 | S3 | b | a |
| S3 | S2 | S4 | a | b |
| S4 | S1 | S4 | a | b |

M2

| | 0 | 1 | 0 | 1 |
|----|----|----|---|---|
| 00 | 00 | 10 | 0 | 0 |
| 01 | 00 | 10 | 1 | 1 |
| 10 | 01 | 11 | 0 | 0 |
| 11 | 01 | 11 | 1 | 1 |

- a) If M is to be serially composite with itself, what are the states of the composite machine?
- b) Give the state and output transition tables of the composite machine.
- 5. i) Find all the upper and lower bounds of the SP partitions given below.

$$\pi_1 = \{\{1, 2\}, \{3\}, \{4\}, \{5\}, \{6\}\}\}$$

$$\pi_2 = \{\{1\}, \{2\}, \{3\}, \{4\}, \{5, 6\}\}$$

$$\pi_3 = \{\{1, 2\}, \{3\}, \{4\}, \{5, 6\}\}$$

$$\pi_4 = \{\{1, 4\}, \{2, 3, 5, 6\}\}$$

ii) Draw the lattice for the above partitions.

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